

Name: Robider Date: \_\_\_\_\_**Functions and Relations****Terms to Know:**

- ⊙ Relation: Any set of input that has an output.
- ⊙ Function: A relation such that every single input has exactly one output.

*The notation of a function is important in higher mathematics such as calculus and in areas which use mathematics such as physics.*

Domain: set of all input values (x-coordinates)

Range: set of all output values (y-coordinates)

Here are a few examples:

- ⊙ Input the number of seconds after the starting gun in a race to get an output of the number of meters the runner has covered.

**Race Chart**

Number of Seconds (input)	1	4	7	8
Meters Covered (output)	5	20	35	40

$$D: \{1, 4, 7, 8\} \quad R: \{5, 20, 35, 40\}$$

- ⊙  $y = x - 6$ , where  $x$  is the place holder (also called a variable) for the input and  $y$  is the place holder for the output.

**Function:  $y = x - 6$**

$x$ (input)	-3	0	7	8
$y$ (output)	-9	-6	1	2

$$D: \{-3, 0, 7, 8\} \quad R: \{-9, -6, 1, 2\}$$

- ⊙ The rule about only **one output** each time is crucial and must not be violated.

**Not a Function**

input	3	2	0	3
output	4	-1	2	-3

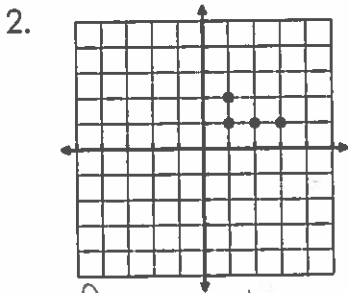
Why is this not a function? input value of 3 was assigned two different outputs

### How do I determine if a relation is a function?

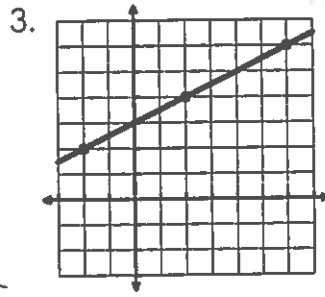
- ⊙ Each input must have exactly one output.
- ⊙ Look at the graph....The vertical line test: No vertical line can pass through two or more ~~points~~ points on the graph.

Examples: Are these relations functions?  $y$

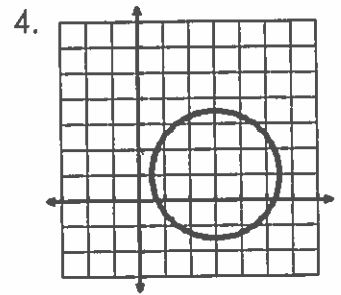
1.  $\{(3,2), (4,3), (5,4), (6,5)\}$  yes. each input has exactly one output



no - fails vertical line test



yes - passes the vertical line test



### Function Notation:

- ⊙ Function notation is a way to name a function. It is pronounced "f of x".
- ⊙  $f(x)$  is a fancy way of writing "y" in an equation.
  - Example:  $f(x) = 2x + 4$  is the same as  $y = 2x + 4$

Function Notation	x-y Notation
$f(x) = 5x + 2$	$y = 5x + 2$
$f(x) = -3x - 7$	$y = -3x - 7$

### Evaluation Functions:

- ⊙ Evaluate  $f(x) = x^2 - 2x + 3$ , when  $x = -3$  and  $x = 4$ .
- $$f(-3) = (-3)^2 - 2(-3) + 3 = 9 + 6 + 3 = 18$$
- $$f(4) = (4)^2 - 2(4) + 3 = 16 - 8 + 3 = 11$$